Automatic Detection and Verification of Solar Features

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Abstract

A fast hybrid system for the automated detection and verification of active regions (plages) and filaments in solar images is presented in this paper. The system combines automated image processing with machine learning. The imaging part consists of five major stages. The solar disk is detected in the first stage using a morphological hit-miss transform, watershed transform and Filling algorithm. An image enhancement technique is introduced to remove the limb darkening effect and intensity filtering is implemented followed by a modified region growing technique to detect the regions of interest (RoI). The algorithms are tested on H-alpha and CA II K3 line solar images that are obtained from Meudon observatory, covering the period from 2nd July 2001 till 4th August 2001. The detection algorithm is fast and it achieves FAR error rate of 67% and FRR error rate of 3% for active regions, and FAR error rate of 19% and FRR error rate of 14% for filaments, when compared with the manually detected filaments in the synoptic maps. The detection performance is enhanced further using a neural network (NN) which is trained on statistical features extracted from the RoI and non-RoI. Using this combination the FAR has dropped to 2% for active regions, and 4% for filaments.

Keywords: Image Processing; Solar Imaging; Morphological Transforms; Neural Networks.

1 Introduction

Observatories and satellites provide Solar images by continuous automated monitoring of the sun. The substantial information about different solar features contained in these images cannot be fully processed manually and require tools developed for the automated recognition of the features of interests.
Solar filaments are one of the features whose detection is very important for understanding solar activity. Evolution and disappearance of filaments are highly associated with Coronal Mass Ejections (CME) [Webb 2000, Gopalswamy 2003] which can excite geomagnetic storms that cause electrical power outages and damages to satellites. On the solar disk filaments look like a dark elongated features on brighter background and can have a lifetime from one to three solar rotations. Although their heliocentric location and their shape do not change grossly there are still visible changes seen in their elongation, position with respect to an active region and magnetic field configuration. Active regions are regions on the solar disk with a very strong magnetic field that is able to confine high temperature gas. Flares are very large explosive events that could occur when the magnetic flux tubes of the active regions are moved around interacting with each other [Harra et al, 2003].

The key to space weather prediction is the accurate detection and monitoring of the evolution of solar features affecting space weather (i.e., Flares, Coronal Mass Ejections (CMEs), etc.). Detecting filaments and active regions can be a precursor for flares or CMEs, which are very energetic phenomena and can cause severe problems for space industry; earth based electromagnetic communications and power systems, radio transmission, space industry and so on. The accurate detection of active regions can provide more insight into the formation, support and disruptions of flares and CMEs [Benkhalil et al, 2003].

There have been previous attempts to apply imaging algorithms to detect solar features. In Gao et al. (2002), local thresholding and region-growing methods were used to detect filament disappearances. In Benkhalil et al. (2003), active regions were detected based on region growing. Filaments were detected in H-alpha images in Shih et al. (2003) using morphological closing operations with multi-directional linear structuring elements to extract elongated shapes. The Singular Spectrum Analysis of signals was used to detect active regions on solar disk, in Lefebvre et al. (2004). In addition, Neural Networks were used in Zharkova et al. (2003) for filament recognition in solar images and in Borda et al. (2002) for flare detection. Qu et al. (2003) experimented and compared Multi-Layer Perceptron (MLP), Radial Basis Function (RBF), and Support Vector Machine (SVM) classifiers for solar flare detection on the solar H-alpha images obtained from the Big Bear Solar Observatory (BBSO). The algorithm introduced here is fast compared to other algorithms and is capable of detecting more than one type of solar features.

In this paper, the aim is to provide robust, fast and accurate automated detection for solar features. In addition, we aim to simplify the detection process, so that the same algorithm can be applied for the detection of different features, with very minimal changes. The detection algorithm is coupled with machine learning to increase the accuracy of detection.

This paper is organised as follows: Section 2 provides information about solar images used in this paper (H-alpha and Calcium II K). The detection of the solar region using the Filling algorithm is described in Section 3. Section 4 is devoted to the limb
darkening removal. The initial detection of RoI using the intensity filtering and the modified region growing algorithm is provided in section 5. The practical implementation is reported in Section 6 and the verification stage is given in Section 7. Finally, the concluding remarks are provided in Section 8.

2 H-alpha and Calcium II K-line Images

H-alpha images (Fig. 1) are captured by observing light from a particular line in the hydrogen spectrum at 6563 Å (red light) [NASA, 2005]. The core of the line is formed between 1200 and 1800 km above the visible surface. The presence of interacting magnetic fields in the chromosphere generates an enormous amount of heat. The heated regions are represented by brighter pixels in the captured H-alpha images. H-alpha images also show many dark filamentary structures on the solar disk, which correspond to magnetic loops reaching up into the solar corona. These features tend to be cooler than the surrounding corona and permit H-alpha absorption to take place, hence their dark appearance [Poppe, 2005].

Full disk images of the Sun at the H-alpha wavelength have been made from the ground since 1926 and have become an integral part of the space weather forecasting effort. In this paper, H-alpha images were obtained from Meudon observatory-France (http://bass2000.obspm.fr). In addition, H-alpha images can be captured using satellites, which would achieve near 100% temporal coverage [Eparvier, 2001]. H-alpha images can be used for examining solar active regions, chromospheric features like filaments, sunspots, and flares.

The Calcium II K-line images are important for solar feature analysis. Singly ionized calcium atoms in the solar chromosphere and upper photosphere form the Calcium II K-line, which is a very broad absorption line at 3933 angstroms (violet light) [UoM, 2005]. The K3 feature, which is the central minimum, is formed at about 2000 km above the visible surface. The two maxima on either side of the K3 minimum are referred to as the K2 peaks and they are formed at height from about 600 to 1500 km above the visible surface. The K1 minima, just outside of the K2 peaks, are formed at about 500 km above the visible surface. In these images (Fig. 1.b), the brighter regions correspond to regions of strong magnetic field [NSO, 2005]. Dark sunspots and filaments are also visible in these images [UoM, 2005].

3 The detection of the solar region

The solar disk is detected using a combination of morphological features. The Filling algorithm [Qahwaji et al, 2001] is designed to detect closed shape objects in digital images. It is based on the morphological hit-miss transform (HMT) [Sonka et al, 1999], used for the edge detection and noise removal, and the morphological watershed transform (WST) used for image analysis. In this
work, the Filling algorithm is used to detect the largest closed shape object in the image, which is the solar disk. Detecting the solar disk is important because it eliminates textual and non-solar information that are contained in the image.

The Filling algorithm was designed to distinguish between the background region that lies outside the object and the region that lies within the object. The algorithm depends on understanding the behaviour of HMT edges and WST lines inside closed and open shape objects. Closed regions have WST lines that divide them into two parts or more. Every WST pixel is surrounded by two horizontal edge pixels, one pixel from the right and one from the left. In addition, the WST lines in closed regions, starts from an edge pixel and ends in an edge pixel [Qahwaji et al., 2001]. These findings can be examined in Fig. 2, where WST is applied to the HMT image of a solar image.

These characteristics are represented in terms of a detection algorithm that starts by finding all the horizontal edges that have WST lines emerging from them. Every WST line that is vertically continuous and ends in another horizontal edge is highlighted, as it may exist inside an object. The Filling algorithm provides valuable information about the shape, size and location of all objects in the image. This information is used to isolate the regions of interest (RoIs). The longest highlighted WST line corresponds to the edges of the solar disk, which is the largest object in these images. The detailed implementation of the algorithm is shown in Fig. 3. For more details on the implementation, the reader can refer to Qahwaji et al. (2001).

4 Limb darkening removal

After the solar disk is detected, limb darkening removal followed by intensity filtering is applied to the H-alpha images in order to detect the candidate pixels for the filaments. Limb darkening removal is important because the limb darkening effect causes the solar background to become darker, which increases the detection of filaments detection. However, this is not a problem for the detection of active regions. Hence, the intensity filtering stage is applied for CA II K3 images without limb darkening removal.

Most solar images suffer from limb darkening which is the gradual decrease in brightness of the disk of the Sun as observed from its centre to its edge, or limb. This phenomenon is readily apparent in photographs of the Sun. Limb darkening occurs because the solar atmosphere increases in temperature with depth. At the centre of the solar disk, an observer sees the deepest and warmest layers that emit the most light. At the limb, only the upper, cooler layers that produce less light can be seen [Encyclopædia Britannica, 2005]. Equation (1) is introduced in Allen (1976) and is used in this paper to remove the limb darkening effect. The Solar limb darkening function is:
\[ \text{Pixel}(x, y) = \frac{\text{Pixel}_0(x, y)}{1-[u \times (1-\cos \theta)]-[v \times (1- \cos^2 \theta)]} \quad (1) \]

Where \( \theta \) represents the angle between Sun’s radius vector and the line of sight through the centre of the disk and \( u \) and \( v \) are constants calculated by using the observation wavelength, in a manner similar to Freeland (2004). \( \text{Pixel}_0(x,y) \) is the initial grey scale value of the processed pixel and \( \text{Pixel}(x,y) \) is the new grey scale value for the same pixel.

In order to find the angle \( \theta \), the centre of the solar disk and its radius (\( R \)) must be determined. The centre of the solar disk can be determined easily using the centre of mass (centroid) method [Baxes, 1994]. The radius (\( R \)) is determined by finding the horizontal and vertical distances towards north, south, west and east separating the centre from the solar limb. The average of these distances is taken to be the radius. The average of the four distances is considered because the shape of the solar disk is not always exactly circular. Angle \( \theta \) is calculated using Equation (2), which depends on distance \( D \) and the radius of the solar disk \( R \), where \( D \) is the shortest distance between the centroid and the processed pixel.

\[ \theta = \arcsin(D / R) \quad (2) \]

Afterwards, the new grey-scale value is calculated for the processed pixel using Equation (1). The contrast enhanced difference between the original and the enhanced image is shown in Fig. 4 to illustrate the effect of removing the limb darkening effect.

### 5 Initial detection of regions of interest

After removing the limb darkening, intensity filtering is applied in order to detect the seeds (candidate pixels) for the desired solar features.

#### 5.1 Seed Selection Using Intensity Filtering

The filaments are darker in colour, which enables an intensity filter with a low threshold to indicate their positions and to eliminate the background and active regions. For the brighter coloured active regions an intensity filter with a high threshold value is used to indicate their positions. The grey scale value of every pixel in the enhanced image is compared against a detection threshold and replaced by a white pixel only if its initial value is smaller than the intensity threshold for filaments and larger than the intensity threshold for active regions. The filtering stage provides two images; the first contains the seeds for active regions while the second
contains the seeds for filaments. In Fig. 5, intensity filtering results for a single H-alpha and CA II K3 images are shown. In this paper H-alpha images are used for the detection of filaments while CA II K3 images are used for the detection of active regions.

The threshold value for each image is found automatically using Equation (3), where, \( \mu \) is the mean, \( \sigma \) represents the standard deviation, and \( \alpha \) is a constant that is determined based on the type of the features to be detected.

\[
\text{Threshold} = \mu \pm (\alpha + (1 - \frac{\sigma}{\mu}) \times \sigma) \quad (3)
\]

For filaments, constant \( \alpha \) is calculated using Equation (4) and (-) sign is used in Equation (3).

\[
\alpha_f = \frac{\mu}{8} \quad (4)
\]

For active regions, constant \( \alpha \) is calculated using Equation (5) and (+) sign is used in Equation (3).

\[
\alpha_a = \frac{255 - \mu}{5} \quad (5)
\]

Equations (4) and (5) are found empirically by taking into account the variance of greyscale values of the solar features in different types of solar images. It is worth mentioning that a thresholding technique is introduced in Gao et al. (2002). For this work, this technique has failed to give good candidates especially for the images that suffer from distortions. The formula introduced in this paper is more complicated but provides better performance. The strength of Equation (3) is that it can be applied to both active regions and filaments just by changing the constant. In the next stages, a region-growing algorithm is modified and compared with that in Benkhali et al. (2003) and Gao et al. (2002) and is followed by a group detection algorithm that is applied to detect the solar features.

5.2 Modified Region Growing Algorithm

The modified region growing technique is applied in order to detect pixels that are regions of interest but have not been detected by intensity filtering. Region growing was applied for the detection of solar regions in Gao et al. (2002) and Benkhali et al. (2003). Our technique combines the region growing techniques suggested by Gao et al. (2002) and Benkhali et al. (2003). It is applied to binary images that result from the intensity filtering stage, where the seeds are simply the white pixels. It is a combination of two major stages: First the adjacent seeds are combined and second unwanted seeds are eliminated. This algorithm provides further
filtering for the unwanted seeds that were detected during the intensity filtering. The intensity filtering detects the seeds after comparing them with a threshold. It does not take into account other seeds (pixels) that were not detected but belong to RoI. The modified region growing is applied to overcome this problem.

5.2.1 Pseudo-Code of the Modified Region Growing Algorithm

1. The percentage of the number of seeds to the total number of pixels in the image is found. The variable size windows and the threshold value are based on the percentage, and are determined by the value of $X$, which is found empirically, as shown in Table I. After $X$ is found, the size of the corresponding window and thresholds are calculated. Window (1) is equal to $(2X+1) \times (2X+1)$, window (2) is equal to $(2X+7) \times (2X+7)$ and the threshold value is equal to $X^2/2$.

2. The area around the seed is scanned for other white pixels. If another white pixel is found in this area, it is connected to the central seed with a straight line as shown in Fig. 6. The details of this procedure are as follows:

   a. In order to connect seeds, a window (Table I – Column (III)) is centred on each seed and the search for other marked pixels within this window is carried out. A simple first-degree polynomial is created to connect the seed to the marked pixel using a false colour. The equation $y=ax+b$ is used to find the coordinates of the connecting seeds, with $a$ being the slope of the straight line and $b$ being the $y$-intercept.

   b. This process continues for all of the seeds. The newly marked false coloured pixels are not taken into account.

3. For all the seeds, the resulting image is processed again with a larger window. This time, another window (Table I – Column (IV)) is centred on the seed and all other pixels (false coloured or not) within this window are counted. If the total number of the pixels inside this area is smaller than the corresponding threshold value (Table I – Column (V)), then the seed in the centre of the window is deleted otherwise all the pixels within the window are marked. This process continues for all the seeds.

5.3 Selection of the Regions of Interest

This stage aims to detect the locations of the desired features after the application of the modified region-growing algorithm. The algorithm starts by detecting the adjacent seeds in each row, as shown in Fig. 7. The row number, the starting column and the ending column are recorded for these pixels. Afterwards, all the vertically adjacent rows are detected and considered as one group (whole feature).
5.3.1 Pseudo-Code for the detection of groups

1. The adjacent seeds in each row are recorded using their row number, the starting column and the ending column number.

2. Each recorded row is highlighted and given index 0 in the beginning of this stage.

3. Before processing each recorded row, if its index is 0 it is given a number starting from 1, which is increased every time this row is processed.

4. All the pixels of the processed row are compared with pixels of other rows to find whether they are vertically adjacent or not. If the rows are vertically adjacent, then the index number of the detected row is examined.
   - If its index number is 0, then it is replaced with the index number of the main row.
   - If its index number is nonzero, then this indicates that this row was processed before. Hence, its number is assigned to the main row and to all the rows that have the same index number as the main row.

5. The 3rd and 4th steps are repeated until all the rows are recursively checked.

6. After all the rows are processed; the rows are checked for their final index numbers. All rows that share the same index number are assumed to be vertically adjacent, and are treated as groups that represent a feature.

7. The locations of the pixels belonging to the detected groups are found and stored in multiple size arrays. The generated arrays contain the detected solar features.

The detection algorithm presented here can be used to process CA II K3 and H-alpha images to provide the exact positions for active regions and filaments. It can be used to detect other solar features (such as sunspots) just by modifying the intensity filtering stage to produce the candidates for this new feature. Examples of the complete implementation of the detection algorithm are shown in Fig. 8 and Fig. 9.

6 The evaluation of performance

The detection algorithm was implemented on solar images obtained from the Meudon observatory-France (Fig. 10 and Fig. 11). These images and a manually constructed synoptic map that contains the locations of solar RoI for any given day can be obtained from http://bass2000.obspm.fr. These synoptic maps were obtained using the subjective analysis of a solar observer. Subjective analysis depends mainly of the experience of the human operator, but it is also affected by fatigue and other human-related factors.
On the other hand, the objective analysis of solar images, which is carried out by the automated detection system, provides consistent performance but its accuracy is usually lower. The detection algorithm finds both solar filaments and active regions in a 1024 × 1024 image in less than three seconds using P4-2.4 G Hz PC with 512 Mbyte RAM. In order to evaluate the detection performance, the following two error rates are introduced [Hong et al, 1997]:

- The false acceptance rate (FAR), which is the probability of a non-RoI being detected as a RoI.
- The false rejection rate (FRR), which is the probability of a RoI not being detected because it is considered to be a non-RoI.

The H-alpha and CA II K3 images available (depending on observing conditions) for the period from 2nd July 2001 till 4th August 2001 were used to evaluate the detection performances for filaments and active regions respectively. The FAR and FRR error parameters are established by comparing the detected RoI, which are generated using the current detection algorithms, with those detected manually and recorded in the synoptic maps.

The results for the detection of active regions are shown in Table II. The first column shows the date for every CA II K3 Line image, while the total number of active regions that are manually detected is indicated in Column II. The FAR and FRR error rates are shown in Columns III and IV, respectively. The FAR error rate represents the percentage of the detected regions that do not contain real active regions. On the other hand, the FRR error rate is the percentage of the active regions that are not detected in the resulting image. The average FAR error rate for all the images of Table II is found to be 67% while the average FRR error rate is 3%.

The results for the detection of filaments are shown in Table III. The first column shows the date of every H-alpha image, while the total number of filaments that are manually detected is indicated in Column II. The FAR and FRR error rates are shown in Columns III and IV, respectively. The average FAR error rate for all the images of Table III is found to be 19% while the average FRR error rate is 26%.

Applying the detection algorithm for the detection of filaments and active regions has resulted in high FAR, which is caused mainly by the threshold of the intensity filtering stage. However, choosing lower thresholds for filaments and higher thresholds for active regions will reduce the FAR but will increase the FRR. To overcome this, machine learning is used to reduce the FAR error rate. Hence, a new stage called the verification stage is added.
7 Verification of solar features using Neural Networks

A verification stage is implemented to enhance the accuracy of the detection. The verification is carried out using a Neural Network (NN) with back propagation training algorithm. The NN training vector is constructed by extracting statistical features characterising RoI and non-RoI. The extracted statistical features are: Mean, standard deviation, range of grey-scale intensities, ratio of dark regions, ratio of bright regions, skew and kurtosis. Calculating the mean and standard deviation is a straightforward process, while other features can be calculated as follow:

- Skewness, which is a data distribution measurement that shows distortion in a positive or negative direction and can be calculated using Equation (8):

\[
Skew = \frac{\sum_{n=0}^{N} [X(n) - \mu]^3}{N\sigma^3}
\]  

(8)

- Kurtosis, which is a measure of the peakedness (broad or narrow) of a distribution and can be calculated using Equation (9):

\[
Kurtosis = \frac{\sum_{n=0}^{N} [X(n) - \mu]^4}{N\sigma^4} - 3
\]  

(9)

- Ratio of the bright regions, which is the ratio of the total number of pixels above a defined threshold value divided by the total number of pixels. The threshold value is equal to the +25% of the calculated mean.

- Ratio of the dark regions, which is the ratio of the total number of pixels below a defined threshold value divided by the total number of pixels. The threshold is equal to -25% of the calculated mean.

- Range of grey scale intensities, which is the difference between the maximum grey-scale value and the minimum grey-scale value, divided (normalized) by 255.

The features for the RoI are extracted from the detected regions after being verified manually with the synoptic maps. The features for the non-RoI are extracted manually and they represent the background regions that contain no RoI (i.e., no filaments or active regions) (Fig. 12). Several experiments are carried out and it was found empirically that the best learning performance is obtained using the following NN topology: 7 input nodes, one hidden layer with 9 nodes and two output nodes. The output nodes indicate whether the detected region is a RoI or not.
The training of the NN is considered to be successful when the NN manages to converge to the normalized system error, which is 0.001. Feature extraction is applied to every region that is detected by the detection algorithm. The seven statistical features are calculated and fed to the NN to determine whether the detected region represents a RoI or not. This approach is implemented on the entire test data and it is found that the average FAR for the detection of active regions has dropped from 67% to 2% and the average FRR has increased to 15% as shown in Table II column V and VI. The average FAR for the detection of filaments has dropped from 19% to 4% and the average FRR has increased to 36% as shown in Table III column V and VI. The increases in FRRs are not desired but acceptable when compared with the great reduction in FARs. These rates can be improved by further training of NN.

8 Conclusions

In this paper, a fast algorithm for the detection of active regions in CA II K3 Line images and filaments in H-alpha images is presented. The detection process consists of five major stages: the detection of the solar region, limb darkening removal, initial detection of regions of interest using intensity filtering, modified region growing and selection of solar features.

The algorithms are tested on solar images that are obtained from the Meudon observatory, covering the period from 2nd July 2001 till 4th August 2001. The detection algorithm is fast and it achieves a FAR error rate of 67% and a FRR error rate of 3%, when compared with the manually detected active regions in the corresponding synoptic maps. In the same manner, applying the detection algorithm on H-alpha images for the same period achieves a FAR error rate of 19% and a FRR error rate of 14%, when compared with the manually detected filaments in the synoptic maps.

The FAR is very high for both cases and a verification stage is added to the current detection technique, to increase the accuracy of the detection process. A Neural Network (NN) is trained on statistical features extracted from the active regions and non-active regions. Using this combination the FAR has dropped to 2%. Another NN is trained on statistical features extracted from filament regions and non-filament regions. Using this combination the FAR has dropped to 4%.

The system introduced in this paper can detect various solar features simultaneously. It takes less than three seconds to detect all the solar features in a 1024 × 1024 image using P4-2.4 G Hz PC with 512 Mbyte RAM. All the imaging stages are shared for the filaments and active regions, except the limb darkening removal. This portability makes the algorithms quite useful and fast for the detection of various types of solar features in different solar images.
In the Future, we would like to modify the existing algorithm to accept different types of solar images (e.g. SOHO MDI Magnetograms and White light images), to detect sunspots and to track solar features over consecutive days. We believe that modifying the detection algorithm to process various types of solar images and comparing the characteristics of the detected and tracked features with recent and historical data can be an important tool for the prediction of space weather activities (i.e., flares and CMEs). These suggestions are supported by the findings in previous research. In Zhou et al. (2003), it was found that 88% of halo CMEs were associated with flares and more than 94% were associated with eruptive prominences/filaments, while 79% of the CMEs were initiated from active regions. This study was conducted on SOHO/LASCO images taken between 1997 and 2001. More recently, Jing et al. (2004) performed a statistical study of 106 filament eruptions taken from BBSO from 1999 to 2003 and their relations to flares and CMEs. It was found that 56% of the filament eruptions were associated with CMEs and active region filament eruptions have a higher flare association.

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References


Table I: The window sizes and threshold values used for the modified Region Growing.

<table>
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<th>%</th>
<th>X</th>
<th>Window (1)</th>
<th>Window (2)</th>
<th>Threshold</th>
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<td>&lt;1</td>
<td>5</td>
<td>11x11</td>
<td>17x17</td>
<td>32</td>
</tr>
<tr>
<td>&lt;3</td>
<td>6</td>
<td>9x9</td>
<td>15x15</td>
<td>25</td>
</tr>
<tr>
<td>=&gt;3</td>
<td>7</td>
<td>7x7</td>
<td>13x13</td>
<td>18</td>
</tr>
</tbody>
</table>

Table II: The false acceptance rate (FAR) and the false rejection rate (FRR) values for selected solar images, representing active region detection (D) and verification (V) processes.

<table>
<thead>
<tr>
<th>Date</th>
<th>Active R.</th>
<th>FAR (D)</th>
<th>FRR (D)</th>
<th>FAR (V)</th>
<th>FRR (V)</th>
</tr>
</thead>
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<td>02/07/2001</td>
<td>21</td>
<td>76%</td>
<td>0%</td>
<td>5%</td>
<td>0%</td>
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<td>03/07/2001</td>
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<td>52%</td>
<td>0%</td>
<td>5%</td>
<td>5%</td>
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<td>04/07/2001</td>
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<td>44%</td>
<td>0%</td>
<td>10%</td>
<td>10%</td>
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<tr>
<td>06/07/2001</td>
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<td>59%</td>
<td>0%</td>
<td>12%</td>
<td>6%</td>
</tr>
<tr>
<td>09/07/2001</td>
<td>16</td>
<td>52%</td>
<td>0%</td>
<td>0%</td>
<td>13%</td>
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<tr>
<td>10/07/2001</td>
<td>19</td>
<td>63%</td>
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<td>0%</td>
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<td>11/07/2001</td>
<td>21</td>
<td>75%</td>
<td>0%</td>
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<td>14%</td>
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<td>15/07/2001</td>
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<td>46%</td>
<td>6%</td>
<td>0%</td>
<td>25%</td>
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<tr>
<td>16/07/2001</td>
<td>16</td>
<td>71%</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
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<td>17/07/2001</td>
<td>18</td>
<td>67%</td>
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<td>0%</td>
<td>11%</td>
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<td>62%</td>
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<td>16</td>
<td>80%</td>
<td>6%</td>
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<td>54%</td>
<td>7%</td>
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<td>14%</td>
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<tr>
<td>24/07/2001</td>
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<td>6%</td>
<td>6%</td>
<td>6%</td>
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Average 17 67% 3% 2% 15%
Table III: The false acceptance rate (FAR) and the false rejection rate (FRR) values for selected solar images, representing filament detection (D) and verification (V) processes.

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